

^{3.1/57} $f(x) = \lfloor x \rfloor$

$\lfloor x \rfloor$ is the greatest integer that is less than or equal to x .

$$f(0) = 0$$

$$f(1.6) = 1$$

$$f(-2.3) = -3$$

$$f(5-2\pi) =$$

$$f(5-6.28) =$$

$$f(-1.28) =$$

$$= -2$$

domain:

$$(-\infty, \infty)$$

range: integers

\mathbb{Z} Zahlen

real numbers:

\mathbb{R}

59) $f(x) = \begin{cases} x^2 + 2x & \text{if } x < 2 \\ 3x - 5 & \text{if } 2 \leq x \leq 20 \end{cases}$

Piecewise-Defined Function

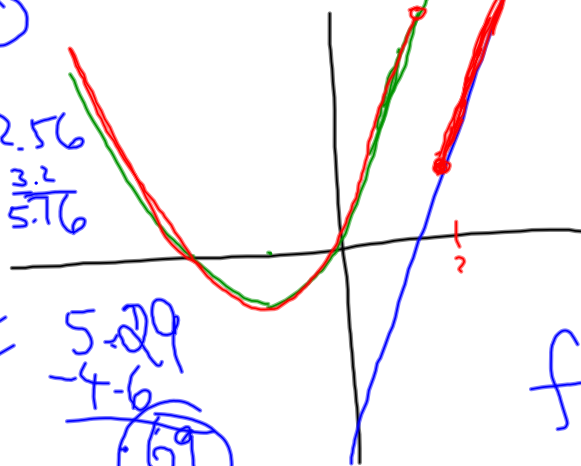
$$f(0) = 0$$

$$f(1.6) = 2.56$$

$$\frac{3.2}{5.16}$$

$$f(-2.3) = \frac{5.29}{-4.6}$$

69



$$f(5-2\pi) = (5-2\pi)^2 - 2(5-2\pi)$$

$$f(15) = 40$$

$$f(21) = \text{undefined}$$

Domain:

$$x \leq 20$$

$$(-\infty, 20]$$

Range: $[-1, \infty)$

636 in 45

$$A = \pi r^2$$

$$d = 2r$$

$$\left(\frac{d}{2}\right) = r$$

$$A = \pi \left(\frac{d}{2}\right)^2$$

$$= \pi \left(\frac{d^2}{2^2}\right) = \frac{\pi d^2}{4}$$

55) $f(x) = -\sqrt{9 - (x-9)^2}$

find "largest domain"

$$\{x \mid (9 - (x-9)^2) \geq 0\}$$

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$$\begin{array}{l} 9 - (x-9)^2 \\ 9 - (x^2 - 18x + 81) \\ 9 - x^2 + 18x - 81 \\ -x^2 + 18x - 72 \\ (x-9)(x-9) \end{array}$$

$$\{x \mid -x^2 + 18x - 72 \geq 0\}$$

$$\begin{array}{r} 72 \\ 1 \cdot 72 \\ 2 \cdot 36 \\ 3 \cdot 24 \\ 4 \cdot 18 \\ 6 \cdot 12 \\ 8 \cdot 9 \end{array}$$

$$\{x \mid x^2 - 18x + 72 \leq 0\}$$

$$\{x \mid (x-6)(x-12) \leq 0\}$$

$$x = 6, 12$$



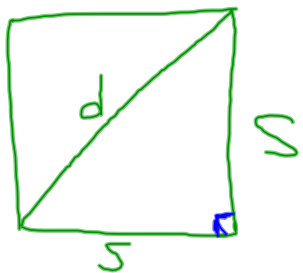
$$\{x \mid 6 \leq x \leq 12\}$$

$$[6, 12]$$

64b) area of a square

$$A = s^2 = \left(\frac{d}{\sqrt{2}}\right)^2 = \frac{(d)^2}{(\sqrt{2})^2} = \frac{d^2}{2}$$

b: in terms of the diagonal



$$d^2 = s^2 + s^2$$

$$d^2 = 2s^2$$

$$\frac{d^2}{2} = s^2$$

$$\frac{d^2}{2} = s^2$$

$$\sqrt{\frac{d^2}{2}} = s$$

$$\frac{\sqrt{d^2}}{\sqrt{2}} = s$$

$$\frac{d}{\sqrt{2}} = s$$

Sign Charts

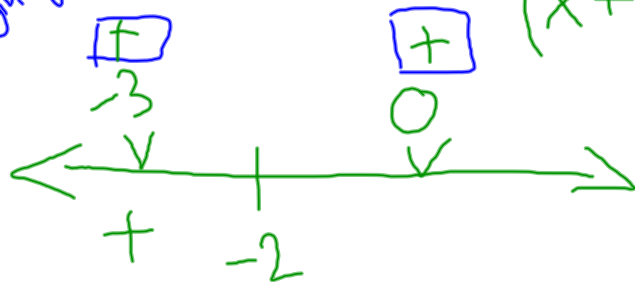
$$x^2 + 4x + 9 \geq 5$$

$$-5 \quad -5$$

$$x^2 + 4x + 4 \geq 0$$

$$(x+2)(x+2) \geq 0$$

sign of $(x+2)(x+2)$



$$x = -2$$

